Granulometric characterization of sediments transported by surface runoff generated by moving storms

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Abstract. Due to the combined effect of wind and rain, the importance of storm movement to surface flow has long been recognized, at scales ranging from headwater scales to large basins. This study presents the results of laboratory experiments designed to investigate the influence of moving rainfall storms on the dynamics of sediment transport by surface runoff. Experiments were carried out, using a rain simulator and a soil flume. The movement of rainfall was generated by moving the rain simulator at a constant speed in the upstream and downstream directions along the flume. The main objective of the study was to characterize, in laboratory conditions, the distribution of sediment grain-size transported by rainfall-induced overland flow and its temporal evolution. Grain-size distribution of the eroded material is governed by the capacity of flow that transports sediments. Granulometric curves were constructed using conventional hand sieving and a laser diffraction particle size analyser (material below 0.250 mm) for overland flow and sediment deliveries collected at the flume outlet. Surface slope was set at 2%, 7% and 14%. Rainstorms were moved with a constant speed, upslope and downslope, along the flume or were kept static. The results of laboratory experiments show that storm movement, affecting the spatial and temporal distribution of rainfall, has a marked influence on the grain-size characteristics of sediments transported by overland flow. The downstream-moving rainfall storms have higher stream power than do other storm types.

1 Introduction

The soil material transported by overland flow is important for water quality management, environmental decision making, urban management and sustainability of ecosystems. The objective of this study is to enhance the understanding of water erosion factors and processes.

The influence of the spatial and temporal distribution of rainfall on surface runoff and associated transport processes on different types of ground cover has long been investigated. However, for a long time, all manner of difficulties have been encountered in characterizing and controlling with precision the parameters that influence runoff. Thus, experiments using rain simulators started to be carried out. Laboratory experiments allowed a better control of parameters and led to improved results. The benefits of using rain simulators for the characterization of surface runoff have been discussed by Meyer (1965), Bryan and Poeseen (1989), Cerda et al. (1997), among others. However, many studies did not take into account the effect of the movement of rainfall caused by the action of wind on runoff. Failure to consider the movement of rainfall (i.e., the combined action of wind and rain) can result in under- or over-estimation of peak discharge (e.g., Jensen, 1984; Singh, 1998; de Lima and Singh, 2002, 2003). The importance of the combined action of wind and rain, especially the changes in rainfall characteristics (e.g., spatial and temporal distribution, trajectory of drops) and runoff (e.g., height of runoff and speed), has been recognized by a number of investigators (e.g., Maksimov, 1964; Yen and Chow, 1968; Wilson et al., 1979; Erpul et al., 1998; Gabriels et al., 1997; Singh, 1998; de Lima and Singh, 1999; Erpul et al., 2000 and 2003, de Lima et al., 2003). Some investigators (e.g., de Lima and Singh, 2002) have thus considered the movement
of rainfall over basins, particularly upstream or downstream. They have found a significant influence of the direction of rainfall on runoff and sediment transport.

Erosion of soil by water is a natural phenomenon that influences the origin and dynamics of landscapes; it thus plays an important role in the evolution of ecosystems. Understanding the factors that affect water erosion are fundamental for planning and designing measures for soil conservation, particularly where the intensive use of soil has been degrading land and water. Erosion of soil by water is caused by the combined and the simultaneous effect of the processes of disaggregating soil aggregates by the impact of rain drops and runoff and then the transport of these aggregates by runoff (e.g., Römkens et al., 1997; Meyer, 1981). Any factor that influences runoff characteristics consequently affects the erosion of soil by water.

Although processes such as infiltration, runoff and water erosion have been extensively studied using rain simulators, the great majority of these studies used constant rainfall intensities, thus differing considerably from the characteristics of natural rainfall, which is highly variable in both time and space (e.g., Huff, 1967; Eagleson, 1978; Sharon, 1980; Willems, 2001). The spatial and temporal distribution of rainfall is one of the main factors affecting runoff on slopes.

This study attempts to characterize the grain-size distribution of sediments carried by runoff, allowing for the evaluation of the influence of rainfall storm movement (upstream, downstream or static) and of the soil flume gradient (which varied as 2%, 7% and 14%) on the grain-size. This evolution, evaluated by grain-size distribution curves, was then related to the respective runoff hydrographs, thus identifying the part of the hydrograph with greater erosive impact on soil; this part could be the rising or falling limb or the peak discharge of the runoff hydrograph.

2 Methodology

The methodology used to conduct the experiments was divided into two phases: (i) Simulation of rainfall events and obtaining the hydrographs of direct runoff; and (ii) characterization of the transported sediments by runoff (e.g., temporal evolution and granulometry analysis).

2.1 Rainfall simulator

Erosion of soil by water has been studied extensively, both in the field and in laboratory, with rain simulators (e.g., Morgan, 1995). The rain simulator (Fig. 2) comprises a constant level reservoir, a pump, a system of hoses, a stand, 2 electric engines, 1 automatic control panel to control the speed at which the apparatus moves, and a sprinkler (nozzles from Spraying Systems Co.) fixed on a connecting rod in the stand 2.20 m above the surface of the flume.

The rainfall used in the laboratory experiments had the spatial distribution presented in Fig. 1 as a consequence of a constant pressure of 2 bar, corresponding to a discharge of 121 l/min. To measure the rainfall intensity distribution under the rainfall simulator, 70 gauges were used in a 0.3×0.3 m² square grid of covering an area of 2.7 m long and 1.8 m wide. Given the flume area and the pre-established duration of rainfall, this discharge is the equivalent of a rainfall intensity of 138 mm/h, which, for Coimbra (Portugal), can be related to a return period of about 2 years. As in other natural situations, the spatial distribution of simulated rainfall is not uniform: in the catchment area affected by rainfall the intensity is higher in some parts and lower in others. This characteristic of rainfall has been described by Bras and Rodrigues-Iturbe (1976), Sivapalan and Wood (1986) and Willems (2001), and others.

Rainfall moving upstream and downstream at a constant speed was simulated over a laboratory soil flume. The rainfall movement was achieved by moving the wheeled stand holding the nozzle over the flume. The static rainfall had the nozzle mounted on the vertical line that contains the geometric centre of the flume.

The experimental apparatus was moved on wheels on a steel rail, powered by 2 electric motors. The speed of the rain simulator was kept at a constant speed of 1.97 m/min, which corresponds to a total of 3.3 litres of water falling on the flume surface. The duration of the static rainfall was determined so as to guarantee a rainfall volume equal to the moving rain events. It should also be noted that the laboratory experiments were performed without wind, and therefore do not entirely represent the real wind-driven rain conditions (no added horizontal wind component). This paper deals mainly with the spatial and temporal distribution of the rainfall, as a consequence of the movement of the rainfall simulators, which is one of the main factors affecting runoff on slopes.

2.2 Soil flume

The soil flume was made of zinc-coated iron and was 3.00 m long, 0.30 m wide and 0.10 m deep. The structure allowed the channel slope to be altered by means of adjustable screws. The surface flow was collected at the lower end of the flume. In this study both the type of rainstorm and the soil flume gradient were varied, the latter by using the following gradients: 2%, 7% and 14%. The slope gradient is one of the critical factors controlling soil erosion caused by runoff (e.g., Bryan and Poesen, 1989).

The sedimentary material used in the laboratory experiments as “soil” was taken from the right bank of the Mondego River, in Coimbra, Portugal. The eroded material was readily available and shows, in situ, important signs of water erosion. The material was taken from a Triassic outcrop, consisting mainly of quartz and feldspar, but also included quartzite, mica and clay minerals. The soil consists of 7%
clay, 9% silt and 84% sand and gravel. The soil texture information is listed in Table 1.

2.3 Laboratory procedure

During experimentation, it was observed that there was always a larger quantity of fine particles transported in the first simulated rains; so each rainfall type was repeated 4 times for observing differences in granulometric characteristics. To ensure identical initial conditions, the soil material placed in the flume was replaced with original soil before each rain type and was subjected to a standard treatment. The soil was first sieved to remove coarser particles and organic material, and then placed in the soil flume in a series of layers to achieve a 0.10 m thick layer of uniform depth. Before each repetition the surface layer’s water content was controlled by imposing a 30 min interval between simulated rainstorm events. The volumetric soil water content was approximately 20% (determined by Time-Domain-Reflectometer measurements) just before the start of each storm event.

The repetition for each type of rainfall was identical. In this study, identical rainfall means events of the same rainfall intensity, the same pattern and the same equivalent drop diameter distribution, and which move in the same direction and at the same speed (de Lima and Singh, 2002). Overland flow and sediment loss caused by each rainfall event were measured by collecting samples every 15 s in metal containers placed at the downstream end of the soil flume. The starting measurement time for each storm event corresponded to the initiation of overland flow at the flume outlet. Rainfall

Table 1. Particle size distribution of the experimental soil.

<table>
<thead>
<tr>
<th>Material</th>
<th>Particle Size (mm)</th>
<th>Distribution (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clay</td>
<td>0–0.0062</td>
<td>6.64</td>
</tr>
<tr>
<td></td>
<td>0.0062–0.0233</td>
<td>3.23</td>
</tr>
<tr>
<td>Silt</td>
<td>0.0233–0.1500</td>
<td>6.30</td>
</tr>
<tr>
<td></td>
<td>0.1500–0.5000</td>
<td>31.60</td>
</tr>
<tr>
<td>Sand and Gravel</td>
<td>0.5000–4.7600</td>
<td>40.72</td>
</tr>
<tr>
<td></td>
<td>4.7600–19.1000</td>
<td>11.51</td>
</tr>
</tbody>
</table>
was simulated under free draining conditions. Solid weight was obtained by drying the samples in order to characterize the temporal evolution of runoff and sediment discharge. The amount of sediment transported by overland flow was estimated by low temperature oven drying of runoff samples.

After drying the runoff samples, the transported sediments underwent grain-size characterization in order to evaluate how their texture evolved over time. There were two distinct phases in this step: one using the laser diffraction particle size analyzer (for particles finer than 0.25 mm), and the other using conventional sieving (for particles coarser than 0.25 mm). The material whose particle size was less than 0.25 mm, suspended in the liquid medium, was analyzed by the equipment, and the other fraction was dried and sieved conventionally.

Soil detachment significantly changes with windward and leeward slopes under wind-driven rains. This means that, apart from the transport capacity of the overland flow, the delivery of the detached particles to the flow will be different when the rainfall is upstream-moving from when it is downstream-moving (Erpul, 2003a, 2005, 2008). In fact the experiments do not entirely represent wind-driven rains. The paper deals more with the spatial and temporal distribution of the rainfall which is a consequence of the combined action of wind and rain.

3 Results and discussion

3.1 Hydrographs and transport of sediments

Figure 3 presents runoff hydrographs (mean and standard deviation for 4 rain events) and their respective transported sediments for different gradients of the soil flume (2%, 7% and 14%) as a function of storm type (storms moving downstream and upstream, and static storms). It is observed that the distribution of both discharge and soil material transported by runoff depends strongly on the storm type. Due to their reduced variability, the upstream-moving rainfall storms yielded runoff hydrographs with a smaller standard deviation than did other rainfall storm types. The same was found for the soil material transported.

The time to start runoff was affected by both the type of storm and the slope of the soil flume. The time was greater for a flume slope with a smaller gradient. The runoff caused by the downstream-moving rainfall started later, because this event began at the upstream end of the flume. However, due to greater infiltration, it produced a smaller runoff volume than did other rainfall storm types. For this type of event, peak discharge was reached sooner and had a higher value.

The upstream-moving storm was the least erosive storm type, with solid transport being less efficient than other storm types. This can be explained because this kind of storm is characterized by runoff hydrographs with earlier rise, lower peak discharge, less steeply-rising limb, and a longer base time when compared with other storm types. The downstream-moving storm was the most erosive for soil in terms of both the amount of material carried by runoff and the maximum flux of sediments. The effect of the static storm was midway between the other two types.

As seen from Figs. 3 and 4, the soil flume slope had little effect on the hydrograph shape and the peak discharge, but it had a strong influence on the transport of sediments. This is because a steeper gradient increases the transport capacity of runoff, regardless of the storm type.

Table 2 shows the main characteristics of hydrographs and the associated solid transport for slopes and types studied.
Table 2. Runoff hydrographs and related sediment characteristics for different types of storms and for the 3 slopes studied.

<table>
<thead>
<tr>
<th>Type of Storm:</th>
<th>Downstream</th>
<th>Upstream</th>
<th>Static</th>
</tr>
</thead>
<tbody>
<tr>
<td>Flume Slope:</td>
<td>2% 7% 14%</td>
<td>2% 7% 14%</td>
<td>2% 7% 14%</td>
</tr>
<tr>
<td>Total Runoff Flow (mL)</td>
<td>2608.47 2960.32 2918.17</td>
<td>2723.79 3079.75 2929.98</td>
<td>2916.20 3157.65 3182.12</td>
</tr>
<tr>
<td>Peak Runoff (mL/s)</td>
<td>41.35 42.31 41.45</td>
<td>20.73 25.28 25.55</td>
<td>36.13 37.58 37.41</td>
</tr>
<tr>
<td>Total Sediments Transported (g)</td>
<td>8.14 46.98 105.98</td>
<td>6.19 12.70 39.50</td>
<td>3.60 29.90 91.13</td>
</tr>
<tr>
<td>Peak Sediments Transported (g/s)</td>
<td>0.152 0.801 1.763</td>
<td>0.092 0.178 0.586</td>
<td>0.098 0.059 0.039</td>
</tr>
<tr>
<td>Time to Peak (s)</td>
<td>112.50 107.00 105.00</td>
<td>99.00 110.75 93.25</td>
<td>95.50 101.82 78.50</td>
</tr>
<tr>
<td>Beginning Runoff Time (s)</td>
<td>90.00 69.50 67.50</td>
<td>31.50 28.25 25.75</td>
<td>33.00 22.00 19.00</td>
</tr>
<tr>
<td>Sediment loss - g/m²</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Time (s)</td>
<td>0 5 10 15 20 25 30 35 40 45</td>
<td>0 50 100 150 200 250 300</td>
<td></td>
</tr>
<tr>
<td>Liquid Flow - mL/s</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Downstream</td>
<td>3 157.65 3 182.12</td>
<td>3 157.65 3 182.12</td>
<td>3 157.65 3 182.12</td>
</tr>
<tr>
<td>Upstream</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Static</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Note: The sediment transport peak did not always coincide with the peak discharge.

Figure 4. Comparison of runoff hydrographs and respective eroded material for the different slopes and storm types.

Figure 5 shows the total amount of soil transported by runoff for different storm types and surface gradients studied. It can be concluded that: (i) a steeper slope increases the transported sediments; and (ii) of the various storm types, the downstream-moving storm is the one with the greatest capacity to transport sediments.

Figure 6 shows the values of peak discharge and respective peak sediment flows for different rainfall storms and soil flume gradients. As with the total amount of soil loss, the maximum flow of sediments, for a particular event, was also affected by the storm type and flume gradient. It was ob-
observed that: (i) the maximum flow of sediments carried by runoff increased with the flume gradient; (ii) peak discharge was more influenced by the storm type than by the flume gradient, and was greater for the downstream-moving storm than for the upstream moving storm.

3.2 Grain-size evolution of sediments transported by runoff

The grain-size evolution of the sediments transported by runoff was investigated. Runoff carried fine material first, and when peak discharge was reached a coarser material was found. In the falling limb of the hydrograph after rainfall ceased, the sediments basically consisted of fine particles because the direct impact of drops was no longer present, strongly reducing the soil detachment capacities of the shallow overland flow sheet. This behaviour was observed for all storm types and flume gradients. However, it was found that the grain-size of the transported sediments was more akin to the original soil when the flume gradient was steeper.

Figure 7 shows the grain-size evolution (% sand, % silt and % clay) of the transported sediments, collected every 15 s, for different storm types and flume gradients (see also the three last rows of Table 2 for the average values). The percentage of coarse material (sand) increased with steepling flume gradient, due to greater flow energy. It was found that the downstream-moving storm had the greatest capacity to transport coarser material, followed by the static storm and then the upstream-moving storm. It can also be observed that the percentage of sand was greater at peak discharge.

Storm movement also affected the characteristics of sediments transported by overland flow. Figures 8, 9 and 10 present granulometric curves of sediments transported by three storm events (rainfall moving downstream and upstream, and static storm), collected at regular time intervals (every 15 s) until runoff ceased. The curves show the sediments evolution over time. This behaviour can also be seen in the path observed in the USDA textural classification chart (triangle).

Figures 8, 9 and 10 show that rainfall storms that moved downstream had granulometric curves that were closer to the curve of the original soil. These figures show that the steeper the flume gradient, the greater the amount of coarse material, in both the initial samples and the samples corresponding to peak discharge. Steeper gradient therefore implies an energy increment and thus greater water erosion now characterized not only in terms of sediment weight but also in terms of grain-size distribution. The downstream-moving rainfall storm had a greater erosive power than other rainfall storms for all surface gradients tested. Furthermore, it can be observed that the sediments transported during the upstream-moving storm, regardless of flume gradient, are composed
of finer material (silt and clay). However, this percentage of fine material decreases as the flume gradient increases. As a consequence, the granulometric curves are further away from the curve of the original soil, compared with the other storm types.

Figure 11 shows the granulometric curve relating to the rising and falling limbs and peak discharge for the 3 types of storms and flume gradients studied. It was found that the rising limb and peak discharge had a greater erosive capacity, and were mostly made up of coarser material, regardless of the flume slope. This can be explained by the raindrop impact effects on overland flow transport capacity. Since the kinetic energy of impacting raindrops is much greater than that of shallow overland flow, it is expected that coarser material is mostly transported during the rising limb.

3.3 Stream power and sediment transport

Quantification of the relation between surface runoff and sediment transport is important to understand the differences between the static storm and moving storms. These non-linear relations are presented in Fig. 12, for the 3 surface gradients, since slope plays an important role in the processes involved. Consequently, regardless of the soil flume slope, the downstream-moving storm is the storm type that possesses...
the highest capacity for the transport of sediments. Static storms have a transport capacity in between downstream and upstream moving storms.

Bagnold (1966) adopted stream power as a theoretical basis for evaluating bedload transport. Since then, stream power has been widely used to better understand such processes in runoff, riverbeds and channels. Stream Power is the energy available to transport sediment. Stream Power per unit length of channel (W m\(^{-1}\)) (e.g., Worthy, 2005; Rose, 2004; Fitzgerald and Bowden, 2006) is:

\[
\Omega = \gamma Q s
\]  

(1)

where \(\gamma\) is the specific weight of water (9.810 N m\(^{-3}\)), \(Q\) is the water discharge (m\(^3\) s\(^{-1}\)), and \(s\) is the energy slope (m m\(^{-1}\)), which may be approximated by the channel bed slope \(s_0\).

If we want to determine stream power for a certain short rainfall event (static or moving under wind), we have to consider the variation of runoff, in time, which represent the hydrologic response of the drainage area (the flume surface in these experiments). For the specific laboratory conditions described in this article, stream power can be calculated as:

\[
\Omega_T = \frac{\sum_{i=1}^{n} Q_i}{n} s_0 L
\]  

(2)

Fig. 9. Granulometric evolution of sediments for 7\% soil flume slope and for 3 storms types: Left: Granulometric curves; and Right: Trajectories in the USDA textural classification chart (triangle).
Fig. 10. Granulometric evolution of sediments for 14% soil flume slope and for 3 storms types: Left: Granulometric curves; and Right: Trajectories in the USDA textural classification chart (triangle).

where $\Omega_T$ is the average stream power for the runoff event (W), $\overline{Q_i}$ is the water discharge for a sampling time interval of 15 s (m$^3$ s$^{-1}$), $L$ is the slope length (m), which is the length of the flume, $s_0$ is the slope of the flume (–) and $n$ is the number of sampling intervals (from the beginning to the end of the runoff hydrograph).

In these experiments we have very shallow overland flow depths and high sediment concentration. It should be noted that the transport capacity of very shallow overland flow is limited and, without raindrop impact, coarse sediments could hardly be transported with these flows (e.g., Moss and Green, 1983; Julien and Simons, 1985; Guy et al., 1987; Kinnell, 1988, 1990 and 1993; Parsons et al., 1998; Zhang et al., 1998). The depth of flow was rather uniform, since significant rills did not appear on the eroding soil surface of the flume.

As water flows down the surface of the flume, the potential energy is converted into kinetic energy. Stream Power is an expression of the rate of energy expenditure or flow strength at a given location. In Fig. 13 stream power is plotted against sediment transported for different storms types and flume slopes. In this figure, the Log-Log relation between stream...
power and sediment transport is shown separately for three different slopes, showing approximately a straight line relationship. In this figure all the experimental data are presented, including the three slopes and the three different storm types (for the sampling time interval of 15 s, which generates: 120 points for the downstream moving storms; 176 points for the upstream moving storms; and 130 points for the static storms). The differences between static and moving storms already mentioned are once more clearly noticeable.

Figure 14 shows total stream power as a function of storm type and flume slope. Total stream power increases with flume slope and is higher for downstream-moving storms for a given slope. This is clearly the result of different rising times, peak discharges and base times affecting the sediment transport processes involved.

4 Conclusions

The following conclusions can be drawn from this study:

1. Comparing rainfall storms moving downstream and upstream, we find that the latter lead to runoff characterized by hydrographs with: (1) earlier rise, (2) lower peak discharge, (3) less steep rising limb, and (4) greater base time. These conclusions were also reached theoretically and experimentally by several investigators (e.g., Singh, 1998; de Lima and Singh, 1999).

2. The paths (sequence of positions, illustrating evolution in time) in the USDA textural classification chart (triangle) associated with upstream-moving storms are different from the paths associated with downstream-moving storms, with finer grain-sizes at the beginning of runoff, evolving to a coarser size as the peak discharge is approached, and to fine particles in the falling limb of
Fig. 12. Relation between the surface runoff and transported sediments as a function of storm type and for the three different flume slopes (applied every 15 seconds and for the 4 repetitions): Top: 2%; Middle: 7%; and Bottom: 14%.

Fig. 13. Relation between the stream power and transported sediments as a function of storm type and for the three different flume slopes (applied every 15 seconds and for the 4 repetitions): Top: 2%; Middle: 7%; and Bottom: 14%.
the hydrograph. The downstream-moving storm with greater initial flow does not evolve in the same way. At first it exhibits a granulometry almost as coarse as the original soil, which then progressively decreases to finer grained sizes.

3. For both the types and flume gradients, the part of the runoff hydrographs that provokes greater soil erosion is the rising limb, as was borne out by the high percentage of coarse material, signifying that the granulometric curve relating to this limb is close to that of the original soil.

4. The downstream-moving rainfall storms have more energy associated with runoff (higher stream power) than do other storm types. Therefore, they are better able to drag coarse particles along, and have the most erosive impact on soil.

5. Stream Power increases with flume gradient; hence a greater percentage of coarse material is carried away. As already reported by other authors, it can be concluded that surface gradient influences solid transport.

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Fig. 14. Stream power as a function of storm type and flume slope.

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