Identification of uranium targets based on airborne radiometric data analysis by using multifractal modeling, Tark and Avanligh 1:50 000 sheets, NW Iran

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Abstract. Airborne geophysical anomaly separation using conventional statistics and the fractal/multifractal concentration-area (C-A) method has been applied to the Tark and Avanligh 1:50 000 sheets in NW Iran. The geophysical survey that resulted in the airborne geophysical data was conducted for uranium exploration in both areas. Selected anomalies were further investigated by using surface radiometric data. Firstly, threshold values to define anomalies were determined and compared by means of conventional statistical methods. Several relatively large anomalies were identified with uranium (U) equal to 1.7 eppm and 1.9 eppm in the Tark and Avanligh areas, respectively; locally these U anomalies have magnitudes exceeding 3.5 eppm in both areas. Log-log plots obtained for the C-A method indicate existence of two separate stages of U enrichment, with a major event being the cause of U concentration values above 6.1 and 3.4 eppm in the Tark and Avanligh areas, respectively. These higher intensity anomalies are located in the northwestern part of the Tark and in the southern part of the Avanligh sheets. In both areas, the C-A anomalies were further investigated using ground radiometric data and XRF analysis revealing higher than 150 and 280 ppm U concentration values in the two areas, respectively. Correlation between the anomalies and geological units show that the anomalies are associated with limestone and sandstone units.

1 Introduction

Airborne geophysical data especially gamma ray spectrometry are utilized to identify uranium targets (Raghuvanshi, 1992). Interpretation of this data is important for mineral exploration, specifically radioactive elements. Several methods have been conducted for interpretation of geophysical airborne data (Abd El Nabi, 1995; Ranjbar et al., 2001; Tourlière et al., 2003; Airo and Mertanen, 2008). Statistical methods are customized for determination of uranium anomaly locations and extensions. Statistical analysis was applied to the airborne spectrometric data for separation of uranium anomalies from background (Abd El Nabi, 1995; Asfahani et al., 2009). In traditional statistical methods, threshold values are calculated in regard to mean and standard deviation or median based on a normal or log-normal distribution. These methods indicate normality or log-normality which does not consider the shape, extent and magnitude of anomalous areas (Rafiee, 2005; Afzal et al., 2010). In addition, geological and geochemical conditions do not have any effect on the geophysical or geochemical anomaly separation from background (Reimann et al., 2005). Fractal geometry is a Non-Euclidean geometry established by Mandelbrot (1983) and has been applied in geosciences and mineral exploration, especially in geophysical and geochemical exploration since 1980s, e.g. Turcotte (1989), Meng and Zhao (1991), Bolviken et al. (1992), Schloz and Mandelbrot (1992), Korvin (1992), Cheng et al. (1994), Barton and La Pointe (1995), Agterberg et al. (1996), Turcotte (1997), Cheng (1999), Li et al. (2003), Turcotte (2004), Daya Sagar et al. (2004), Dimri (2005) and
Shen et al. (2009). In this study, concentration-area (C-A) fractal method was used in order to explain the geophysical airborne data, including U (eppm) from the Tark and Avanligh 1:50 000 sheets, NW Iran. Ultimately, results from C-A fractal method for the U element were compared with geological particulars and surface spectrometry surveys.

2 Concentration-area fractal method
Cheng et al. (1994) proposed concentration-area (C-A) method which is employed to define the geophysical background and anomalies. The method has the general form as follow

\[ A(\rho \leq \upsilon) \propto \rho^{-a_1}; A(\rho \geq \upsilon) \propto \rho^{-a_2} \]  

(1)

where \( A(\rho) \) denotes the area with concentration values greater than the contour value \( \rho \), \( \upsilon \) represents the threshold and \( a_1 \) and \( a_2 \) are characteristic exponents. The breaks between straight line segments in C-A log-log plot and the corresponding values of \( \rho \) are known as thresholds to separate geophysical values into different components representing different causal factors such as, lithological differences, geochemical processes and mineralizing events (Lima et al., 2003). The C-A method serves to depict the relationship between element concentration values and geological data. The most useful feature of the C-A method is its capability to compute anomaly thresholds (Goncalves et al., 2001).

Multifractal models are utilized to quantify patterns such as geophysical data. Fractal and multifractal modeling are widely applied to eliminate the different mineralized zones (Cheng, 2007). Multifractal theory could be interpreted as a theoretical framework that explains the power law relationships between areas enclosing concentrations below a given threshold value and the actual concentrations itself. To demonstrate and prove that data distribution has a multifractal nature, an extensive computation is required (Halsey et al., 1986; Evertz and Mandelbrot, 1992). This method has several constrains especially when the boundary effects on irregular geometrical data sets are involved (Agterberg et al., 1996; Goncalves, 2001; Cheng, 2007; Xie et al., 2010). Multifractal modelings in geophysical and geochemical exploration help to find exploration targets and mineralization potentials in different types of deposits (Yao and Cheng, 2011). The C-A method seems to be equally applicable to all cases which means that geophysical distributions mostly satisfy the properties of a multifractal function. There is some evidence that geophysical and geochemical data distributions have fractal behavior in nature, e.g. Bolviken et al. (1992), Turcotte (1997), Goncalves (2001), Gettings (2005), Li and Cheng (2006) and Afzal et al. (2010). This theory improves the development of an alternative interpretation validation and useful methods to be applied to geophysical distributions analysis.

3 Geological setting of the case studies
Both study areas are located in a major Iranian magmatic belt named Urumia-Dokhtar, which hosts many metallic deposits (Afzal et al., 2010). There are several prospects and one Pb-Zn-Cu mine named Baichehbagh. The Tark and Avanligh 1:50 000 sheets are situated in Eastern Azerbaijan, Eastern Mianeh as depicted in Fig. 1. Regional geological studies in these areas by Lotfi (1975) revealed that major lithological units are Eocene, Miocene and Oligocene magmatic and volcanosedimentary rocks. Magmatic units consist of quartz diorite, granite and syenite, as illustrated in Fig. 1 (Lotfi, 1975; Zia Zarifi, 2009). Miocene sedimentary units include marl, sandstones, conglomerates, siltstones and limestones in SE part of the area. There are several metamorphic rocks including andalosalite schist, mica schist and marbles (Fig. 1). Light limestone field observations in these sheets show a potential for radioactive elements based on Zia Zarifi (2009). Additionally, sandstone and shale units illustrate uranium enrichment in Tark 1:50 000 sheet (Zia Zarifi, 2009).

4 Geophysical airborne analysis
23 000 Geophysical airborne data were collected by Austrex Co. in a grid with 1000 × 500 m distance between air route surveys during 1976 to 1978. Line spacing between flight lines is 500 m with line direction of 41 degrees and sample intervals of 1 s. Detected parameters of these data include U\textsubscript{235}, Th\textsubscript{232} and K\textsubscript{40}.

4.1 Statistical analysis
One of the most important methods to separate background from different anomalies is the method based on classical statistics. This method is depended on data distribution (Davis, 2002). Different anomalies can be separated in normal distribution, but geophysical and geochemical data do not have normal distribution in most of the cases, e.g. Abd El Nabi, 1995; Ranjbar et al., 2001; Davis, 2002; Li et al., 2003; Rafiee, 2005 and Afzal et al., 2010. Uranium histograms were drawn for Tark and Avanligh 1:50 000 sheets, as presented in Fig. 2. Uranium distribution in Tark sheet is not normal but normal distribution is present in Avanligh sheet. Based on statistical method, uranium threshold in Tark 1:50 000 sheet is equal to mean and there are two societies, namely background and anomaly. Threshold value for uranium based on radiometric data is 2.17 eppm and different anomalies cannot be separated in this sheet (Table 1). According to the normal distribution of U airborne data in Avanligh sheet, different anomalies were recognized by using formulas based on mean (\( M \)) and standard deviation (SD). Uranium threshold value is equal to summation of mean and standard deviation which is 2.59 eppm. Low intensity and high intensity anomaly
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Uranium distribution maps in these sheets were generated by Surfer8 software in terms of inverse distance squared (IDS), and uranium was classified to different populations based on classical statistics method, as illustrated in Fig. 3. The studied areas were gridded to 250 × 250 m cells for evaluation of uranium distribution in both sheets. Uranium anomaly in Tark sheet is huge with respect to its size. Based on this method, different grades of anomalies cannot separate in Tark area. Anomalies of uranium in Avanligh area are situated in small parts of northern, southern and specifically in SE parts of this sheet. High intensity anomalies, more than 4.68 eppm, are located in very small parts of southern and SE area (Fig. 3).

4.2 C-A method

C-A log-log plots of uranium were constructed in Tark and Avanligh 1:50000 sheets, as depicted in Fig. 4. Geophysical populations were divided based on linear segments and breakpoints in these log-log plots, as shown in Fig. 4. Uranium distribution in Tark area indicates a multifractal model.

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**Table 1.** Statistical parameters of radiometric geophysical raw data in Tark area.

<table>
<thead>
<tr>
<th>Statistical parameter</th>
<th>U (eppm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
<td>2.17</td>
</tr>
<tr>
<td>Median</td>
<td>2.02</td>
</tr>
<tr>
<td>SD</td>
<td>0.84</td>
</tr>
<tr>
<td>SV</td>
<td>0.70</td>
</tr>
<tr>
<td>Maximum</td>
<td>10.23</td>
</tr>
<tr>
<td>Minimum</td>
<td>0.12</td>
</tr>
</tbody>
</table>

SD: standard deviation, SV: sample variance.

**Table 2.** Statistical parameters of radiometric geophysical raw data in Avanligh area.

<table>
<thead>
<tr>
<th>Statistical parameter</th>
<th>U (eppm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
<td>2.13</td>
</tr>
<tr>
<td>Median</td>
<td>2.10</td>
</tr>
<tr>
<td>SD</td>
<td>0.46</td>
</tr>
<tr>
<td>SV</td>
<td>0.21</td>
</tr>
<tr>
<td>Maximum</td>
<td>4.81</td>
</tr>
<tr>
<td>Minimum</td>
<td>0.62</td>
</tr>
</tbody>
</table>

SD: standard deviation, SV: sample variance.
Uranium distribution maps in these two areas were generated by Surfer 8, as revealed in Fig. 5. Uranium high intensity anomalies, higher than 6.1 eppm, are situated in NE of Tark 1:50000 sheet and moderate intensity anomalies, between 3.5 and 6.1 eppm, are located in central, north and NE parts of this area. High intensive anomalies, higher than 3.4 eppm, occur in small parts in south and SE in Avanligh 1:50000 sheet, as represented in Fig. 5. Moderate intensive anomalies (1.9–3.5 eppm) are situated in northerm and SE parts of this sheet, as depicted in Fig. 5.

Table 3. Thresholds of uranium (eppm) in Tark and Avanligh 1:50000 sheet based on C-A fractal method.

<table>
<thead>
<tr>
<th></th>
<th>Tark</th>
<th>Thresholds</th>
</tr>
</thead>
<tbody>
<tr>
<td>Avanligh</td>
<td>1.9</td>
<td>Low intensity threshold</td>
</tr>
<tr>
<td></td>
<td>2.6</td>
<td>Moderate intensity threshold</td>
</tr>
<tr>
<td></td>
<td>3.4</td>
<td>High intensity threshold</td>
</tr>
</tbody>
</table>
anomalies, between 3.5 and 6.1 eppm, are located in central, north and NE parts of this area. High intensive anomalies in Avanligh area. In addition, Miocene and rhyodacite host U anomalies, specifically the high intensity anomalies in NW of Tark area illustrate that there is a positive correlation between anomalies derived via C-A method and surface radiometrical surveying in Table 4. Based on this study, anomalies associated with red sandstone are siltstone, conglomerates, tuffaceous layers units and marls in Tark 1:50 000 sheet. Miocene limestones, Oligocene rhyolite and rhyodacite host U anomalies, specifically the high intensive anomalies in Avanligh area. In addition, Miocene sedimentary units have a good correlation with U anomalies obtained from C-A fractal method in Tark area. However, volcanic rocks are abundant in Avanligh 1:50 000 sheet which can be a source rock in the north part of the area. Major U anomalies derived by C-A model are situated in red

5 Control with geological particulars, ground radiometric surveying and XRF analysis

Several high and moderate intensive anomaly results from C-A model were examined and controlled by ground radiometric surveying. Surface radiometric data surveyed from Tark and Avanligh are 10 and 5 points, respectively (Table 4). Ground radiometric data collected from C-A moderate anomalies in Tark sheet show U concentration between 32.6 and 80.2 eppm. Spectrometric data from high intensive anomalies in NW of Tark area illustrate that there is U higher than 100 eppm (Table 4). Radiometric data surveyed from high intensive anomalies of Avanligh sheet certify U higher than 250 eppm. Moreover, surface radiometric data collected from moderate intensity anomalies are between 103 and 140 eppm. The results reveal there is a positive correlation between anomalies derived via C-A method and surface radiometrical surveying in Table 4. Based on this study, anomalies associated with red sandstone are siltstone, conglomerates, tuffaceous layers units and marls in Tark 1:50 000 sheet. Miocene limestones, Oligocene rhyolite and rhyodacite host U anomalies, specifically the high intensive anomalies in Avanligh area. In addition, Miocene sedimentary units have a good correlation with U anomalies obtained from C-A fractal method in Tark area. However, volcanic rocks are abundant in Avanligh 1:50 000 sheet which can be a source rock in the north part of the area. Major U anomalies derived by C-A model are situated in red

Miocene sandstones and limestones in Tark and Avanligh 1:50 000 sheets, respectively.

Collected samples from these anomalous points were analyzed by XRF method. Chemical analysis shows that the high intensity anomalous parts obtained by C-A method have U concentration higher than 150 ppm in 86-AZ-TA-04, 86-AZ-TA-06, 86-AZ-TA-09 and 86-AZ-TA-09 (Table 4). U concentrations from collected samples of Avanligh area illustrate the high intensity anomalies with the U grade of higher than 280 ppm, as depicted in Table 4.
6 Conclusions

Study on Tark and Avanligh 1:50 000 sheets reveal the potential use of the C-A method for geophysical airborne anomaly separation as an appropriate tool for geophysical and mineral exploration. The advantages of this method are in its simplicity and easy computational implementation, as well as the possibility to compute a numerical value of the anomalous threshold, which is the most fundamental criteria for cross examination of information with numerical data from different sources, generally used in airborne radiometric data.

Log-log plots in both of the areas show a multifractal model for U. Uranium anomalies result from C-A method and statistical methods were compared in Tark and Avanligh areas. Anomalies resulting from classical statistics methods show only an anomaly in many parts, but most anomalous parts from C-A method are low intensity, between 1.7 and 3.5 epmp. High and moderate intensive anomalies are situated in few parts in central and NE of the area. Uranium anomalies resulting in Avanligh area based on classical statistics are similar to anomalies from C-A method because uranium distribution in this sheet is normal. High and moderate intensity anomalous parts from both methods are correlated in southern, especially in SE parts of this area. According to correlation between geological particulars and uranium anomalies obtained from C-A method, Miocene sedimentary units and Oligocene magmatic rock types host the anomalies in Tark and Avanligh 1:50 000 sheets. Moreover, high intensive anomalies occur in limestones and red sandstones in the Avanligh and Tark areas, respectively.

There is a very good correlation between the calculated anomalous threshold values and the range of concentrations obtained by the ground radiometric surveying, especially for U in these areas. High intensity anomalous parts, obtained from C-A method, in Tark area show there are concentrations higher than 100 epmp in surface radiometric data. Surface radiometric data from Avanligh depicted higher than 250 epmp for high intensity anomalies resulted by multifractal model. Based on these studies, uranium targets were identified in NW of Tark and southern part of Avanligh 1:50 000 sheets. Also, results of analyzed samples by XRF method reveal uranium concentrations are higher than 150 and 280 ppm in Tark and Avanligh 1:50 000 sheets, respectively.

It may be easy to study geophysical airborne anomalies with the C-A method although multifractal nature of C-A log-log curves can be a sufficient way for geophysists to conduct such research in order to find targets with enriched radioactive elements. The developments in multifractal theory and its utilization are highly recommended for stochastic simulation of geophysical distributions.

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References


Table 4. The coordinates of sampling points in Tark and Avanligh areas.

<table>
<thead>
<tr>
<th>Sample name</th>
<th>C-A anomaly intensity</th>
<th>U (epmp)</th>
</tr>
</thead>
<tbody>
<tr>
<td>86-AZ-TA-01</td>
<td>Moderate</td>
<td>32.6</td>
</tr>
<tr>
<td>86-AZ-TA-02</td>
<td>Moderate</td>
<td>37.0</td>
</tr>
<tr>
<td>86-AZ-TA-03</td>
<td>Moderate</td>
<td>55.4</td>
</tr>
<tr>
<td>86-AZ-TA-04</td>
<td>High</td>
<td>107.6</td>
</tr>
<tr>
<td>86-AZ-TA-05</td>
<td>Low</td>
<td>13.1</td>
</tr>
<tr>
<td>86-AZ-TA-06</td>
<td>High</td>
<td>200.3</td>
</tr>
<tr>
<td>86-AZ-TA-07</td>
<td>Low</td>
<td>6.3</td>
</tr>
<tr>
<td>86-AZ-TA-08</td>
<td>Moderate</td>
<td>80.2</td>
</tr>
<tr>
<td>86-AZ-TA-09</td>
<td>High</td>
<td>112.5</td>
</tr>
<tr>
<td>86-AZ-TA-10</td>
<td>High</td>
<td>300.4</td>
</tr>
<tr>
<td>86-AZ-AV-01</td>
<td>Moderate</td>
<td>132.4</td>
</tr>
<tr>
<td>86-AZ-AV-02</td>
<td>Moderate</td>
<td>139.9</td>
</tr>
<tr>
<td>86-AZ-AV-03</td>
<td>High</td>
<td>298.6</td>
</tr>
<tr>
<td>86-AZ-AV-04</td>
<td>High</td>
<td>279.3</td>
</tr>
<tr>
<td>86-AZ-AV-05</td>
<td>Moderate</td>
<td>103.3</td>
</tr>
</tbody>
</table>


Rafiee, A.: Separating geochemical anomalies in stream sediment media by applying combination of fractal concentration-area model and multivariate analysis (Case study: Jel-e-Barez 1:100,000 Sheet, Iran), 20th World Mining Congress Proceeding, Iran, 461–470, 2005.


